

# An Argumentation Framework for Decision Making

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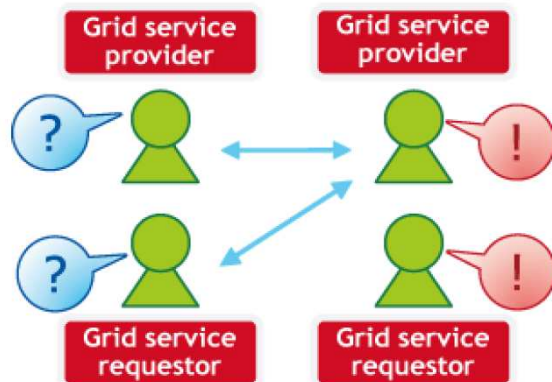
supported by the Sixth Framework IST programme of the EC, under the 035200 ARGUGRID project.

# Outline

- 1 ARGUGRID
- 2 Argumentation
- 3 Assumption-based argumentation framework
- 4 Argumentation-based decision making
- 5 Quantitative argumentation-based decision making
- 6 Conclusions & Future works
- 7 Questions ?

# ARGUmentation as a foundation for the semantic GRID

## Project Aims:



- Enact the reasoning and decision making processes and negotiation required for dynamic composition of Grid resources and services into executable workflows, using argumentative agents to support grid service providers and requestors.
- Impact business and business practices by empowering grid-enabled e-business applications where multiple service requestors and providers exist.

# ARGUGRID Objectives & Partners

- Provide a new model for argumentative agents populating and evolving within a trusted grid.
- Provide a new model for the specification, creation, operation and dissolution of VOs over the grid using argumentation.
- Design an architecture for the semantic grid to support argumentative agents and VOs.
- Develop a grid-based platform to support the implementation of models and architecture and assess the approach.
- Experiment with and evaluate the models, architecture and platform in the context of concrete applications for e-business.



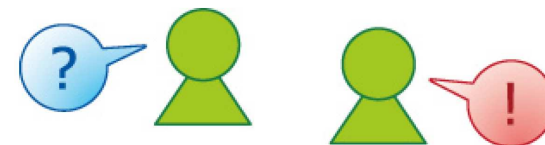
# Outline

- 1 ARGUGRID
- 2 **Argumentation**
- 3 Assumption-based argumentation framework
- 4 Argumentation-based decision making
- 5 Quantitative argumentation-based decision making
- 6 Conclusions & Future works
- 7 Questions ?

# Overview of argumentation

Argumentation is:

- a conceptualisation of nonmonotonic reasoning;



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- a conceptualisation of nonmonotonic reasoning;
- a process of construction and comparison of arguments for and against certain conclusions formalized by an **argumentation framework** [Dung 95] , *i.e.*

- Arguments

- abstract entities



- Attack relation

- Status of arguments

# Overview of argumentation

Argumentation is:

- a conceptualisation of nonmonotonic reasoning;
- a process of construction and comparison of arguments for and against certain conclusions formalized by an **argumentation logic** [Prakken & Sartor 97] , *i.e.*

- **Underlying logic**

- Arguments

- abstract entities
- logical structures

- **Attack relation**

- Status of arguments



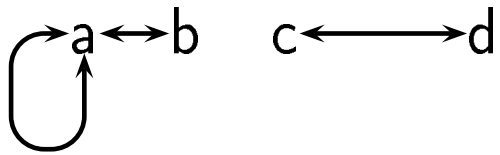
# Overview of argumentation

Argumentation is:

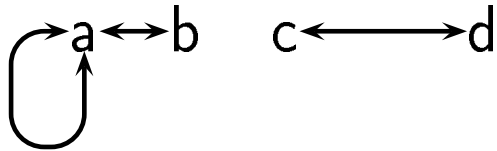
- a conceptualisation of nonmonotonic reasoning;
- a process of construction and comparison of arguments for and against certain conclusions formalized by an **preference-based argumentation logic** [Amgoud & Cayrol 02], *i.e.*
- **Underlying logic**
- **Arguments**
  - **abstract entities**
  - **logical structures**
- **Attack relation**
- **Priority relation**
- **Status of arguments**



# Abstract argumentation framework



# Abstract argumentation framework



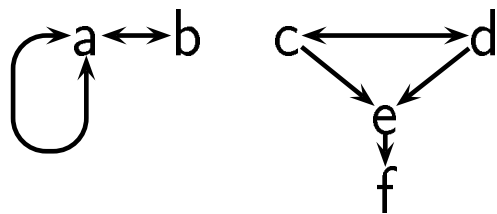
- $\emptyset$  is ground;
- $\{b, c\}$  are  $\{b, d\}$  preferred;
- $\{b\}$  is the maximal ideal set.

## Definition ([Dung, Kowalski & Toni 06])

A set  $X$  of arguments is :

- **admissible** iff  $X$  does not attack itself and  $X$  attacks every argument  $Y$  such that  $Y$  attacks  $X$ ;
- **preferred** iff  $X$  is maximally admissible;
- **complete** iff  $X$  is admissible and  $X$  contains all arguments  $x$  such that  $X$  attacks all attacks against  $x$ ;
- **grounded** iff  $X$  is minimally complete;
- **ideal** iff  $X$  is admissible and it is contained in every preferred sets.

# Abstract argumentation framework



- $\{b, c, f\}$  are  $\{b, d, f\}$  preferred;
- $\{b\}$  is the maximal ideal set and  $\{b\} \subset \{b, f\} \subset \{b, c, f\} \cap \{b, c, f\}$

## Definition ([Dung, Kowalski & Toni 06])

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# The statements

- $\mathcal{L}$  a logic language

## Definition ([Prakken & Sartor 97])

A theory  $\mathcal{T}$  is an extended logic program, *i.e* a finite set of rules:

$$R : L_0 \leftarrow L_1, \dots, L_j, \text{not } L_k, \dots, \text{not } L_m$$

$\text{head}(R) = L_0$ .

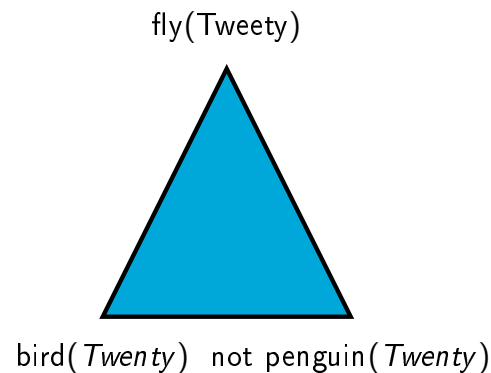
$\text{body}(R) = \{L_1, \dots, \text{not } L_m\}$ .

- $\mathcal{I}$  is an incompatibility relation amongst sentences in  $\mathcal{L}$ 
  - $\mathcal{I}(b_1, \neg b_1)$  and  $\mathcal{I}(\neg b_1, b_1)$ ,
  - $\mathcal{I}(b_1, \text{not } b_1)$

# Argument as 'proof'

Forms of arguments:

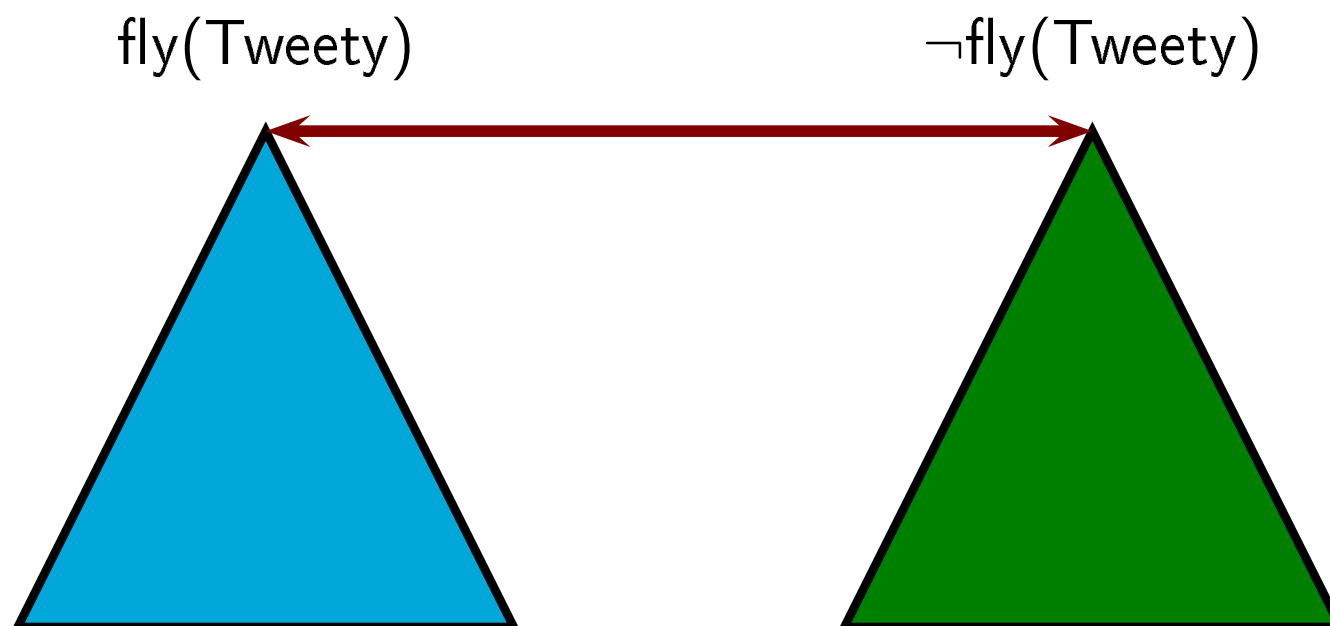
- An **abstract entity** with an unspecified logic,  
 $A = \text{'Tweety flies because it's a bird'}$ ;
- A **pair** (Premises, Conclusion),  
 $A = (\{\text{bird(Tweety)}, \text{bird}(X) \rightarrow \text{fly}(X)\}, \text{fly(Tweety)})$ ;
- A deduction **sequence** of rules and facts  
 $A = (f_1(\text{Tweety}), r_1(\text{Tweety}))$ ;
- An inference **tree** grounded in premises;



# Rebutting, undermining and undercutting attacks

Rebutting attack conflicting conclusions:

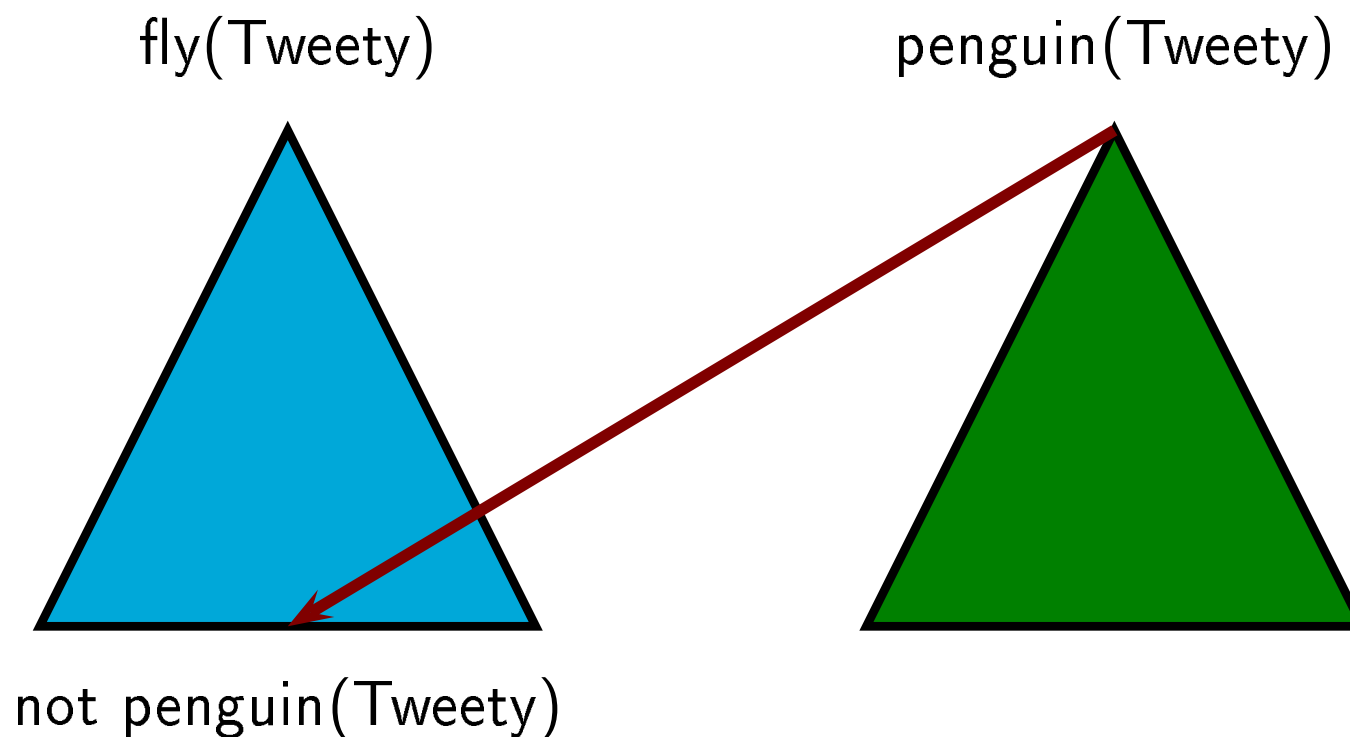
- *Tweety flies because it is a bird;*
- *Tweety doesn't fly because it's a penguin.*



# Rebutting, undermining and undercutting attacks

**Undermining** attack non-provable assumptions:

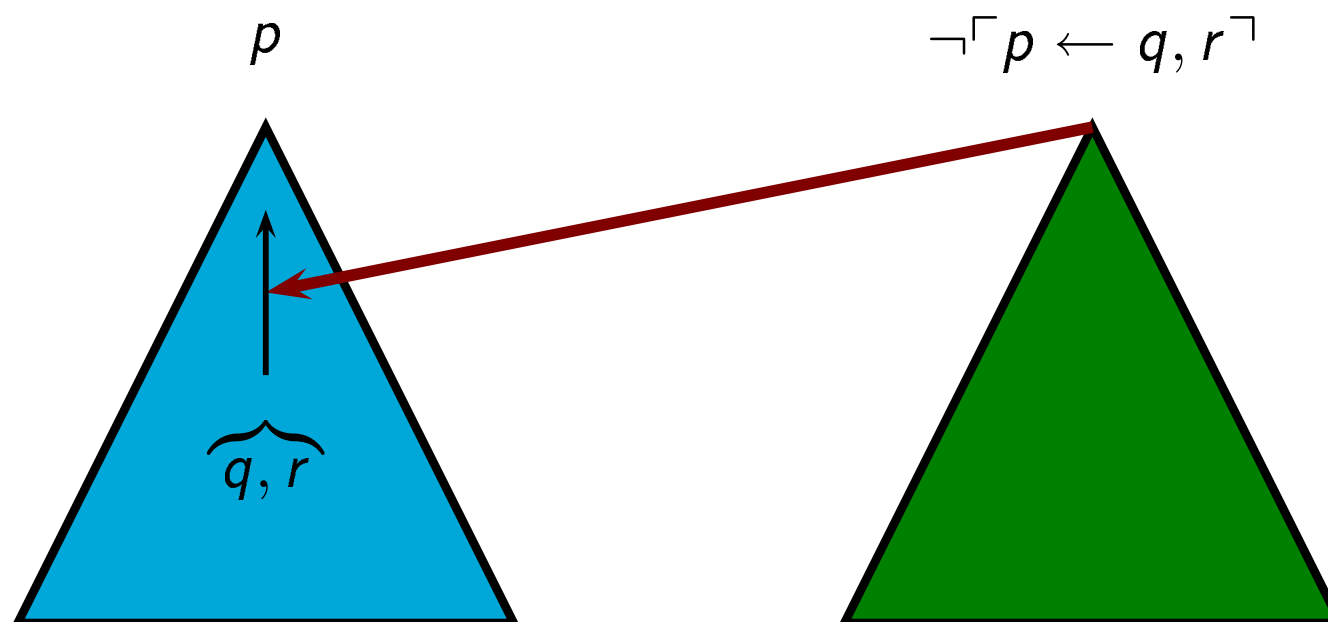
- *Tweety flies because it is a bird and it is not provable that Tweety is a penguin;*
- *Tweety is a penguin.*



# Rebutting, undermining and undercutting attacks

Undercutting attack intermediate step:

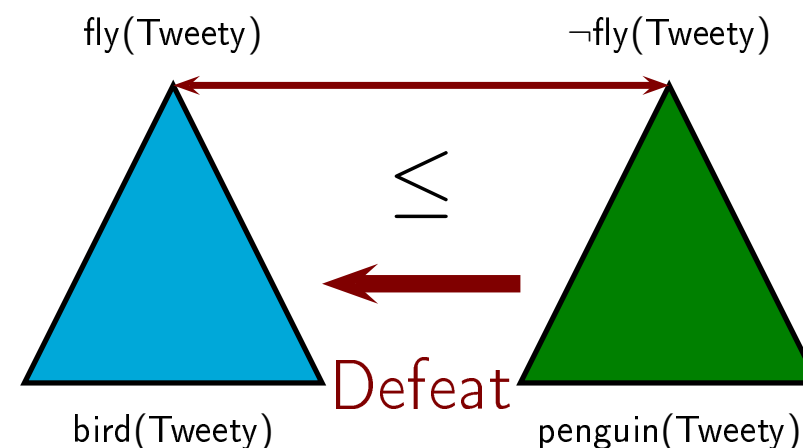
- *Tweety flies because all the birds I've seen fly;*
- *I've seen Tux, it's a bird and it doesn't fly.*



# How to evaluate the strengths of arguments?

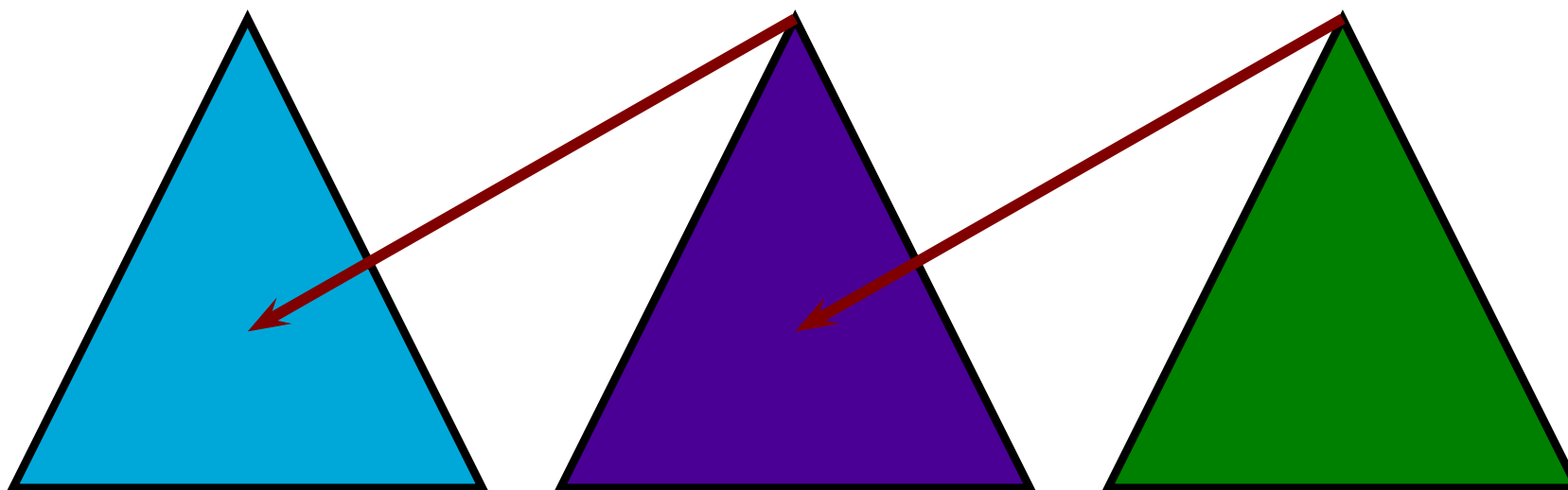
Some domain-independent principles of commonsense reasoning:

- the last link principle [Prakken & Sartor 97];
- the weakest link principle [Amgoud & Cayrol 02];
- the specificity principle [Simari & Loui 92].



# From the defeat relation to the status of arguments

- Defeat relation focus on two arguments not on a dispute, eg



# Burden of proof rather than correspondence with reality

(Declarative) Model-theoretic Semantic

Completeness



Soundness

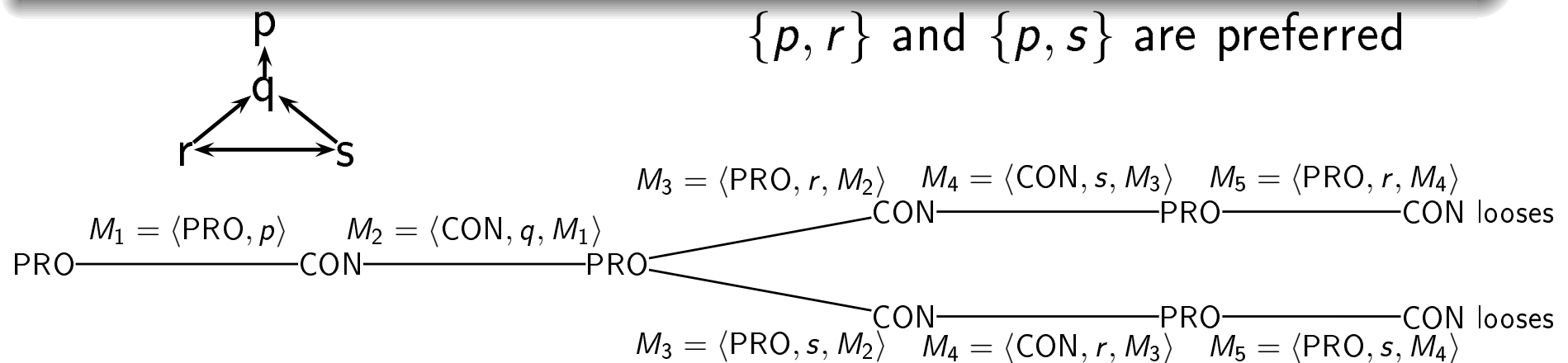
(Procedural) Dialectical Proof Procedure

# Dialectical enquiry

## Definition

A Two-Party Immediate Respond Dispute (TPI) is defined s.a.:

- both parties are allowed to repeat PRO;
- PRO is not allowed to repeat CON;
- CON is allowed to repeat CON in a different dispute line.



## Theorem

*Soundness and completeness of TPI for the sceptically preferred semantics.*

# Take away argumentation technics

**Argumentation framework** is made of:

- Dialectical proof procedure
- Model-theoretic semantics
- Defeat relation
- Priority/Contradictory relation
- Arguments
- Underlying logic

**Argumentation** is a promising approach for:

- decision-making, *i.e.* reasoning with inconsistent information;
- dialogue, *i.e.* facilitating rational interaction;
- collective decision making, *i.e.* reach an agreement.

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# An abstract argumentation framework [Dung, Kowalski & Toni 06]

- An Assumption-based argumentation framework  
 $ABF = \langle \mathcal{L}, \mathcal{R}, \mathcal{A}, - \rangle =$ 
  - $(\mathcal{L}, \mathcal{R})$  a deductive system *i.e.*
    - $\mathcal{L}$  a formal language
    - $\mathcal{R}$  set of inference rules, eg  $p \leftarrow q, r$
  - $\mathcal{A}$  a set of candidate assumption
  - $\bar{p}$  is the contrary of  $p$
- Abstract argument  $A$   
 $\Leftrightarrow$  Tight deductions supported by sets of assumptions  $A \vdash \alpha$ .
- $A$  attacks  $B$   
 $\Leftrightarrow A \vdash \alpha, B \vdash \beta, \text{ and } \alpha = \bar{\delta} \in B$ .

# An example of ABF

- $ABF = \langle \mathcal{L}, \mathcal{R}, \mathcal{A}, - \rangle =$ 
  - $\mathcal{L} = \{a, b, c, d, \neg a, \neg b, \neg c, \neg d\}$
  - $\mathcal{R} = \left\{ \begin{array}{ccc} \neg b & \leftarrow & a \\ & \nearrow & \neg a \\ & & b \end{array} \quad \begin{array}{l} d \longrightarrow \neg c \\ \neg d \longleftarrow c \end{array} \right\}$
  - $\mathcal{A} = \{a, b, c, d\}$
  - $\bar{a} = \neg a, \bar{b} = \neg b, \bar{c} = \neg c, \bar{d} = \neg d$
- Attack relations:
  - $\{a\}$  attacks itself;
  - $\{a\}$  and  $\{b\}$  attack each other.
- Model-theoretic semantics:
  - $\emptyset$  is ground;
  - $\{b, c\}$  are  $\{b, d\}$  preferred;
  - $\{b\}$  is the maximal ideal set.

# Admissible beliefs derivations example

$$ABF = \langle \mathcal{L}, \mathcal{R}, \mathcal{A}, - \rangle =$$

- $\mathcal{L} = \{a, b, c, d, \neg a, \neg b, \neg c, \neg d\}$

- $\mathcal{R} = \left\{ \begin{array}{ccc} \neg b & \swarrow & \neg a \\ & a & \nearrow \\ & & b \end{array} \quad \begin{array}{l} d \rightarrow \neg c \\ \neg d \leftarrow c \end{array} \right\}$

- $\mathcal{A} = \{a, b, c, d\}$

- $\bar{a} = a, \bar{b} = b, \bar{c} = c, \bar{d} = d$

Is  $\neg a$  an admissible belief?

Proponent	Opponent	Ass support. P	Culprit chosen in O
$\{\neg a\}$	$\{\}$	$\{\}$	$\{\}$
$\{b\}$	$\{\}$	$\{b\}$	$\{\}$
$\{\}$	$\{\{\neg b\}\}$	$\{b\}$	$\{\}$
$\{\}$	$\{\{a\}\}$	$\{b\}$	$\{\}$
$\{\neg a\}$	$\{\}$	$\{b\}$	$\{a\}$
$\{\}$	$\{\}$	$\{b\}$	$\{a\}$

# Credulous and Sceptical Argumentation Prolog Implementation

- Written in Prolog by Dorian Gaertner and Francesca Toni
- Available at  
<http://www.doc.ic.ac.uk/~dg00/casapi.html>
- The main procedure is  
`run(derivationtype, outputmode, numberofsolutions)`  
with:
  - the first argument is the type of dispute derivation, eg ab (for admissible belief);
  - the second argument determines the output mode: (s)ilent or (n)oisy.
  - the third argument indicates whether (1) or (a)ll solutions are required.

# A good example is better than a long explanation

```
:- compile('casapi.pl').
```

```
myRule(nb, [a]).
```

```
myRule(na, [a]).
```

```
myRule(na, [b]).
```

```
myRule(nc, [d]).
```

```
myRule(nd, [c]).
```

```
myAss([a, b, c, d]).
```

```
toBeProved([na]).
```

```
contrary(na, a).
```

```
contrary(nb, b).
```

```
contrary(nc, c).
```

```
contrary(nd, d).
```

```
-----
```

```
run(ab, s, a).
```

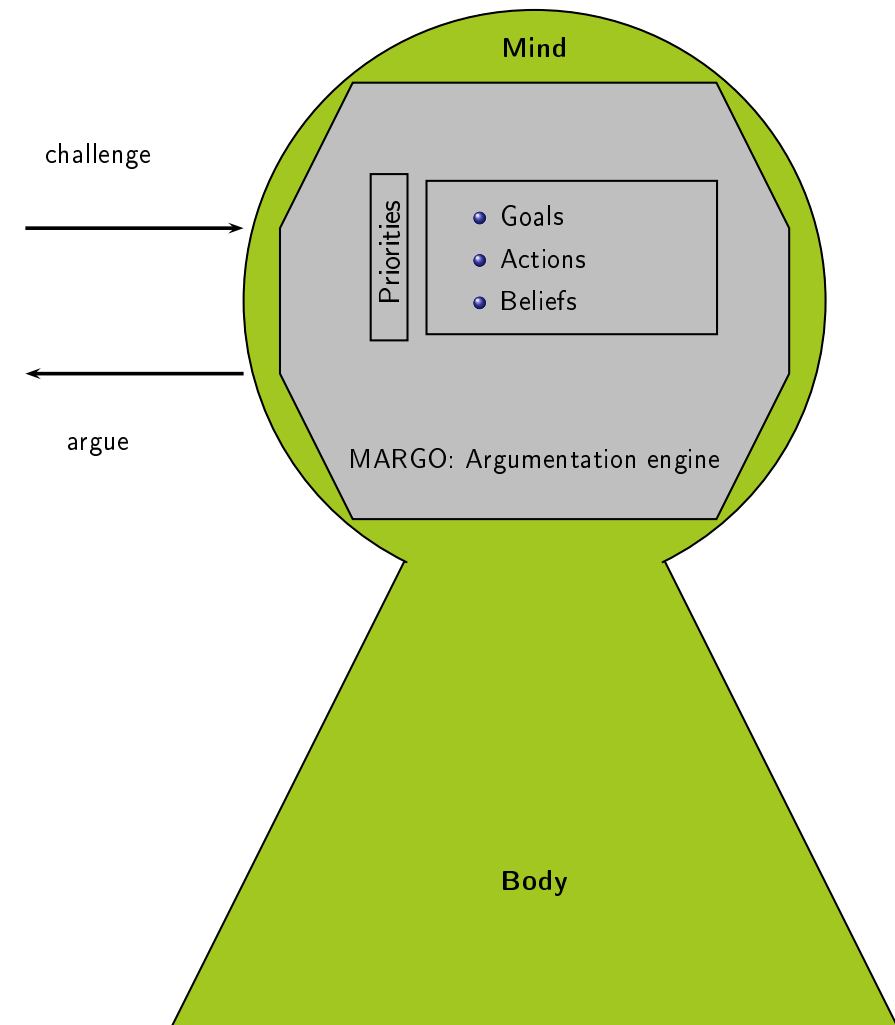
```
FINISHED, one defence set is: [b, b]
```

# Outline

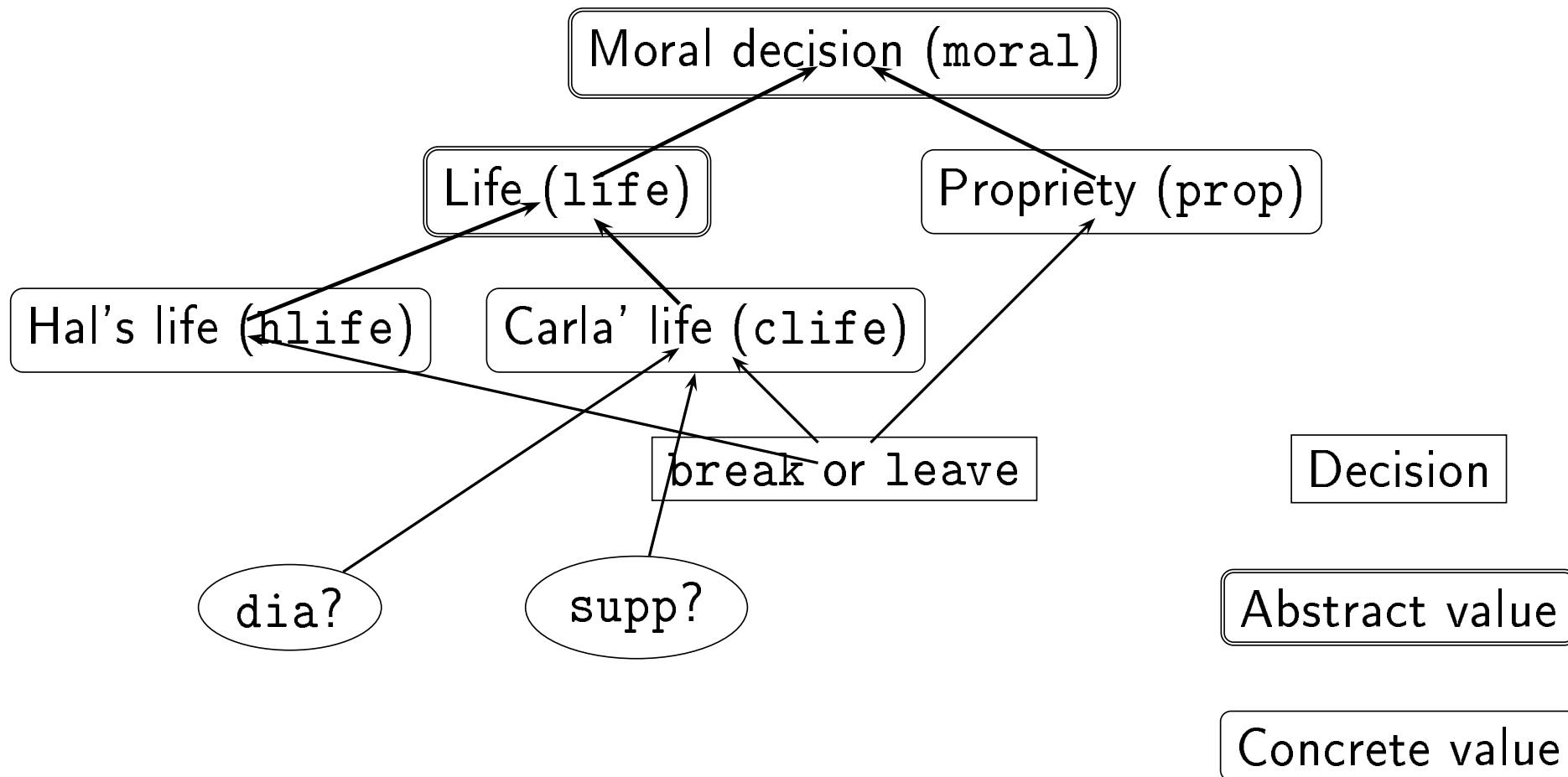
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# Outlook: Agents' mind (WP2)

- Design
  - state-of-mind (knowledge, goals, actions)
  - qualitative priorities (probabilities, preferences, utilities)
- Argumentation-based decision-making
- Implementation
  - MARGO: a Prolog prototype



# Abstract representation of the problem: influence diagram



# Data structures and priorities: hierarchies of conflicting rules

The theory compiles:

- **goal rules** such as  $R_{012} : g_0 \leftarrow g_1, g_2$
- **epistemic rules** such as  $R_{012} : b_0 \leftarrow b_1, \neg b_2$
- **decision rules** such as  $R_{110} : g_1 \leftarrow D(a_1), b_0$

Different priorities for different rules:

- the priority over **goal rules** comes from **preferences**,  
eg  $R_1 : g_0 \leftarrow g_1$  has priority over  $R_2 : g_0 \leftarrow g_2$
- the priority over **epistemic rules** comes from **probabilities**,  
eg  $F_1 : dia \leftarrow$  has priority over  $F_2 : \neg dia \leftarrow$
- the priority over **decision rules** come from **expected utilities**,  
eg  $R_{11} : g_1 \leftarrow D(a_1), b_1$  has priority over  $R_{12} : g_1 \leftarrow D(a_1), b_2$

# A walk through the example

$$\begin{array}{l} \overline{F_1 : dia \leftarrow} \\ \uparrow \\ \overline{F_3 : \neg dia \leftarrow} \end{array}$$

$$\begin{array}{l} \overline{R_{22} : prop \leftarrow D(leave)} \\ R_{31} : hlife \leftarrow D(break) \\ R_{41} : clife \leftarrow D(leave) \\ R_{42} : clife \leftarrow D(break), supp, dia \\ \overline{R_{21} : prop \leftarrow D(break)} \\ R_{32} : hlife \leftarrow D(leave) \\ R_{43} : clife \leftarrow D(break), dia \end{array}$$

$$\begin{array}{l} \overline{R_{012} : moral \leftarrow life, prop} \\ R_{134} : life \leftarrow hlife, clife \\ \overline{R_{01} : moral \leftarrow life} \\ R_{13} : life \leftarrow hlife \\ \overline{R_{02} : moral \leftarrow prop} \\ R_{14} : life \leftarrow clife \end{array}$$

# Structure of arguments: abductive tree

## Definition

An argument  $A = \langle \text{conc}, \text{premise}, \text{hyp} \rangle$  is:

- 1 **hypothetical**, *i.e.* built upon an hypothesis

$$\text{sent}(A) = \text{hyp}(A)$$

$$A = \langle D(\text{break}), \emptyset, [D(\text{break})] \rangle \text{ or } A = \langle \text{supp}, \emptyset, [\text{supp}] \rangle$$

- 2 **trivial**, *i.e.* built upon an unconditional ground statement

$$\text{sent}(A) = \text{premise}(A)$$

$$A = \langle \text{dia}, [\text{dia}], \emptyset \rangle \text{ or } A = \langle \neg \text{dia}, [\neg \text{dia}], \emptyset \rangle$$

- 3 **tree**, *i.e.* built upon a top rule where all literals in the body are the conclusions of subargument s.a:

- $\text{sent}(A) = \bigcup_{A_i = \text{subarg}(A)} \text{sent}(A_i) \cup \text{body}(R)$

- $\neg \mathcal{I} (\bigcup_i \text{sent}(A_i))$  and  $\neg(\text{conc}(A) \mathcal{I} \text{sent}(A_i))$ .

$$B_1^4 = \langle \text{clife}, (D(\text{leave})), ((D(\text{leave}))) \rangle$$

$$A_2^4 = \langle \text{clife}, (D(\text{break}), \text{supp}, \text{dia}), (D(\text{break}), \text{supp}) \rangle$$

$$A_3^4 = \langle \text{clife}, (D(\text{break}), \text{dia}), (D(\text{break})) \rangle.$$

# Interaction: choice between different explanations

## Definition (Attack relation)

$\text{attacks}(A, B)$  iff  $\text{conc}(A) \mathcal{I} \text{sent}(B)$

⇒ build homogeneous explanations:

- $B_1^4 = \langle \text{clife}, (D(\text{leave})), ((D(\text{leave}))) \rangle;$
- $A_2^4 = \langle \text{clife}, (D(\text{break}), \text{supp}, \text{dia}), (D(\text{break}), \text{supp}) \rangle;$
- $A_3^4 = \langle \text{clife}, (D(\text{break}), \text{dia}), (D(\text{break})) \rangle.$

# Interaction: choice between different explanations (cont.)

## Definition (Hypothesis size)

- ① if  $A$  is a hypothetical argument, then  $\text{hypsize}(A) = 1$ ;
- ② if  $A$  is a trivial argument, then  $\text{hypsize}(A) = 0$
- ③ if  $A$  is a tree argument then  

$$\text{hypsize}(A) = \sum_{A' \in \text{subarg}(A)} \text{hypsize}(A').$$

## Definition (Strength relation)

$A_1$  a hypothetical argument, and  $A_2, A_3$  two built arguments:

- ①  $A_2 \succ^A A_1$ ;
- ② If  $(\text{top}(A_2) \prec \text{top}(A_3)) \wedge \neg(\text{top}(A_3) \prec \text{top}(A_2))$ , then  
 $A_3 \succ^A A_2$ ;
- ③ If  $(\text{top}(A_2) \sim \text{top}(A_3)) \wedge (\text{hypsize}(A_2) \leq \text{hypsize}(A_3))$ ,  
then  $A_2 \succ^A A_3$ ;

# Interaction: choice between different explanations (cont.)

## Definition (Defeat relation)

**$A$  defeats  $B$**

- 1 attacks  $(A, B)$
- 2  $\neg(B \succ^A A)$ .

- $B_1^4 = \langle \text{clife}, (D(\text{leave})), ((D(\text{leave}))) \rangle$ ;
- $A_2^4 = \langle \text{clife}, (D(\text{break}), \text{supp}, \text{dia}), (D(\text{break}), \text{supp}) \rangle$ ;
- $A_3^4 = \langle \text{clife}, (D(\text{break}), \text{dia}), (D(\text{break})) \rangle$ .

Since

- $\text{top}(A_3^4) \prec (\text{top}(B_1^4) \sim \text{top}(A_2^4))$ ,
  - $\text{hypsize}(B_1^4) = \text{hypsize}(A_3^4) = 1$  and  $\text{hypsize}(A_2^4) = 2$ ,
- $B_1^4$  defeats  $A_2^4/A_3^4$  and  $A_2^4 \succ^A A_3^4$ .

# Semantics: status of arguments/alternatives

## Definition (Acceptability)

A set  $X$  of arguments is :

- **admissible** iff  $X$  does not attack itself and  $X$  attacks every argument  $Y$  such that  $Y$  attacks  $X$ ;
  - **preferred** iff  $X$  is maximally admissible;
  - **ideal** iff  $X$  is admissible and it is contained in every preferred sets.
- 
- The semantics is:
    - either *credulous*, eg admissible;
    - or *sceptical*, eg ideal, or sceptically preferred semantics.

## Definition (Suggestion)

The decision  $D(a_1)$  is **suggested** iff  $D(a_1)$  is a hypothesis of one argument in an admissible set.

# Procedure and its implementation: relax goals requirement and make hypotheses

```

File Edit Options Buffers Tools Prolog Prolog-help Complete In/Out Signals Help
% ===== %
% DIABETIC DILEMMA %
% ===== %
:- compile('../src/margo.pl').
%moral
goalrule(r012,moral,[life, prop]).
goalrule(r01,moral,[life]).
goalrule(r02,moral,[prop]).
%life
goalrule(r134,life,[hlife, clife]).
goalrule(r13,life,[hlife]).
goalrule(r14,life,[clife]).
%prop
decisionrule(r21, prop, [d(breaking)]).
decisionrule(r22, prop, [d(leaving)]).
%hlife
decisionrule(r31, hlife, [d(breaking)]).
decisionrule(r32, hlife, [d(leaving)]).
%clife
decisionrule(r41, clife, [d(leaving)]).
decisionrule(r42, clife, [d(breaking), supply, diabetic]).
decisionrule(r43, clife, [d(breaking), diabetic]).
%diabetic
epistemicrule(f1,diabetic,[]).
epistemicrule(f2,nodiabetic,[]).
%priority
supergoalpriority([[r012], [r01], [r02]]).
goalpriority([[r134], [r13], [r14]]).
decisionpriority(r22,r21).
decisionpriority(r31,r32).
decisionpriority(r41,r43).
decisionpriority(r42,r43).
epistemicpriority(f1,f2).
%decision
decisions([d(breaking), d(leaving)]).
incompatibility(supply,nosupply).

#####
# Welcome to MARGO - #
# (A Multiattribute ARGumentation framework for Opinion explanation) #
# available at http://margo.sourceforge.net in GPL #
# #
# Please select the goal or the belief you want to challenge. #
# admissibleArgument(+CONCLUSION, ?PREMISES, ?HYPOTHESIS) #
# #
# Developed in 2007 by Maxime Morge and Paolo Mancarella and #
# supported by the 6th Framework IST programme of the EC, #
# under the 035200 ARGUGRID project. #
#####

% ../src/margo.pl compiled 0.00 sec, 56,360 bytes
% /home/morge/Pisa/Impl/MARGO/examples/halcarla2.pl compiled 0.01 sec, 82

Yes
?- admissibleArgument(moral,PREMISES,SUPPOSITIONS).

PREMISES = [life]
SUPPOSITIONS = [d(breaking), supply] ;

No
?- admissibleArgument(life,PREMISES,SUPPOSITIONS).

PREMISES = [hlife, clife]
SUPPOSITIONS = [d(breaking), supply] ;

No
?- admissibleArgument(clife,PREMISES,SUPPOSITIONS).

PREMISES = [d(leaving)]
SUPPOSITIONS = [d(leaving)] ;

No
?-

```

--- halcarla2.pl Top (1,0) (Prolog[SWI])---4:54 0.19--- -1:\*\* \*prolog\* Bot (15,0) (Inferior Prolog: run)---4:54 0.19-----

# Take away MARGO (Multicriteria ARGumentation framework for Opinion justification)

*A argumentation framework for practical reasoning*

↪ *Formalization of a decision making*

- Influence diagram

↪ *Abstract representation*

- Goal/Decision/Epistemic rules

↪ *Specific data structures*

- Priority over epistemic/goal/decision rules

↪ *Intuitions about probability/preferences/expected utilities*

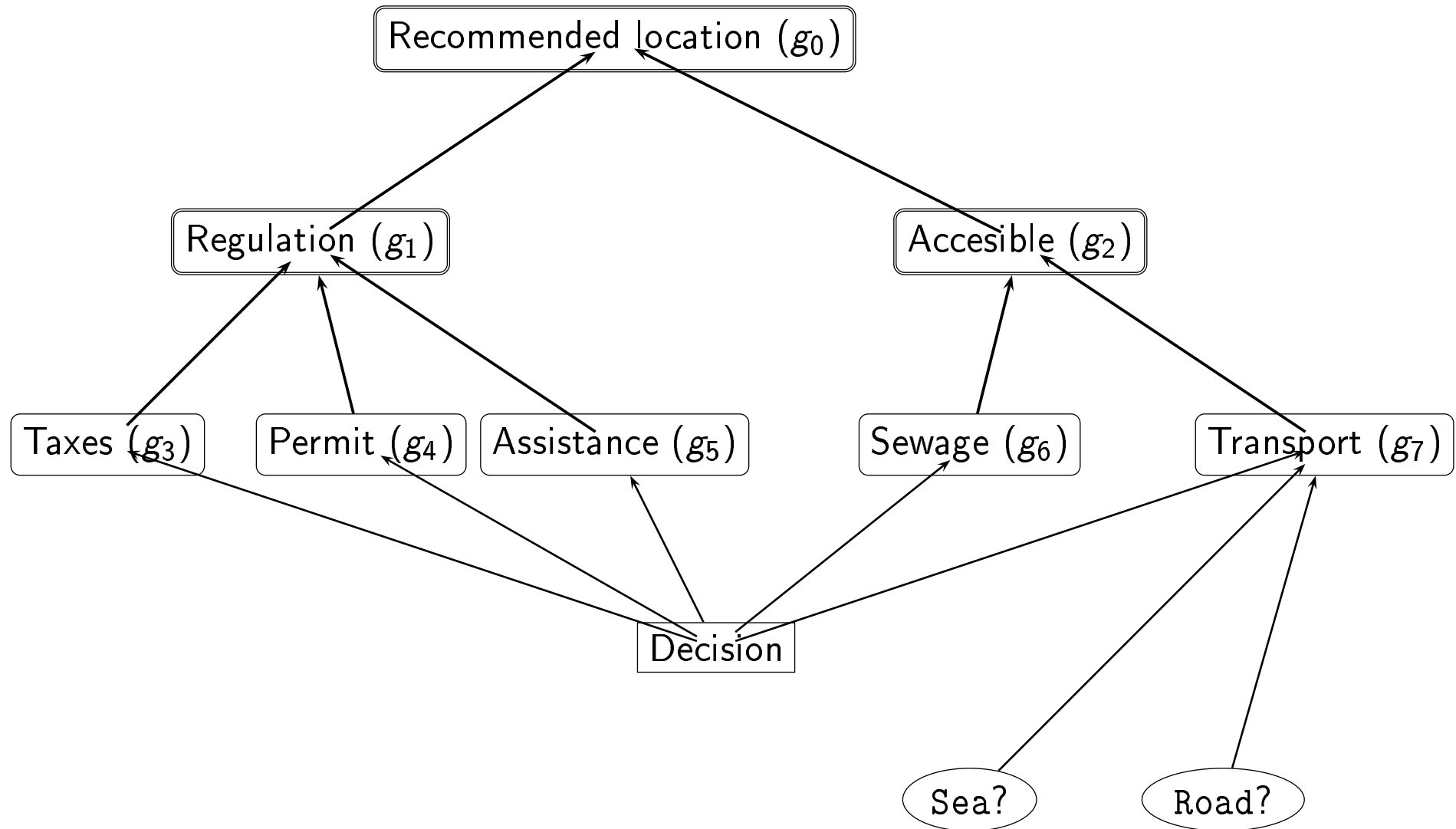
- Abductive tree argument

↪ *Interaction-based explanation of the decision*

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- 7 Questions ?

# Influence diagram



# Epistemic/Goal/Decision theory

$\prec$	$R$	$c(R)$
↑	$R_{012} : g_0 \leftarrow g_1, g_2$	$c(R_{012}) = 1$
	$R_{01} : g_0 \leftarrow g_1$	$c(R_{01}) = 6/10$
	$R_{02} : g_0 \leftarrow g_2$	$c(R_{02}) = 4/10$
↑	$R_{1345} : g_1 \leftarrow g_3, g_4, g_5$	$c(R_{1345}) = 1$
	$R_{135} : g_1 \leftarrow g_3, g_5$	$c(R_{135}) = 8/10$
	$R_{134} : g_1 \leftarrow g_3, g_4$	$c(R_{134}) = 8/10$
	$R_{13} : g_1 \leftarrow g_3$	$c(R_{13}) = 6/10$
	$R_{145} : g_1 \leftarrow g_4, g_5$	$c(R_{145}) = 4/10$
	$R_{14} : g_1 \leftarrow g_4$	$c(R_{14}) = 2/10$
	$R_{15} : g_1 \leftarrow g_5$	$c(R_{15}) = 2/10$
↑	$R_{267} : g_2 \leftarrow g_6, g_7$	$c(R_{267}) = 1$
	$R_{27} : g_2 \leftarrow g_7$	$c(R_{26}) = 1/2$
	$R_{26} : g_2 \leftarrow g_6$	$c(R_{27}) = 1/2$

$\prec$	$R$	$c(R)$
↑	$R_{31} : g_3 \leftarrow D(\text{london})$	$c(R_{31}) = 6/10$
	$R_{32} : g_3 \leftarrow D(\text{pisa})$	$c(R_{32}) = 4/10$
↑	$R_{42} : g_4 \leftarrow D(\text{pisa})$	$c(R_{42}) = 7/10$
	$R_{41} : g_4 \leftarrow D(\text{london})$	$c(R_{41}) = 3/10$
↑	$R_{52} : g_5 \leftarrow D(\text{pisa})$	$c(R_{52}) = 5/10$
	$R_{51} : g_5 \leftarrow D(\text{london})$	$c(R_{52}) = 5/10$
↑	$R_{61} : g_6 \leftarrow D(\text{london})$	$c(R_{61}) = 5/10$
	$R_{62} : g_6 \leftarrow D(\text{pisa})$	$c(R_{62}) = 5/10$
↑	$R_{71}(x) : g_7 \leftarrow D(x), \text{Sea}(x)$	$c(R_{71}(x)) = 6/10$
	$R_{72}(x) : g_7 \leftarrow D(x), \text{Road}(x)$	$c(R_{72}(x)) = 4/10$

$\prec$	$R$	$c(R)$
↑	$F_1 : \text{Road}(\text{pisa}) \leftarrow$	$c(F_1) = 8/10$
	$F_2 : \neg \text{Road}(\text{pisa}) \leftarrow$	$c(F_1) = 2/10$
↑	$F_3 : \text{Sea}(\text{pisa}) \leftarrow$	$c(F_3) = 7/10$
	$F_4 : \neg \text{Sea}(\text{pisa}) \leftarrow$	$c(F_4) = 3/10$

# Interaction: choice between different explanations (cont.)

## Definition (Weight)

- ① if  $A$  is a hypothetical argument, then  $\text{wei}(A) = 1$ ;
- ② if  $A$  is trivial and built upon  $F \in \mathcal{T}$ , then  $\text{wei}(A) = c(F)$
- ③ if  $A$  is a tree built upon  $R \in \mathcal{T}$ , then:

- ① either  $R$  is an epistemic rules of the form  
 $R : B_0 \leftarrow B_1, \dots, B_n$  with  $n \geq 0$ , then

$$\text{wei}(A) = c(R) \times \prod_{i=1}^n \text{wei}(A_i);$$

- ② or  $R$  is a decision rules of the form  
 $R : g \leftarrow D, B_2, \dots, B_n$  with  $n \geq 0$ , then

$$\text{wei}(A) = c(R) \times \prod_{i=1}^n \text{wei}(A_i);$$

- ③ otherwise  $R$  is a goal rule of the form  
 $R : g_0 \leftarrow g_1, \dots, g_n$  with  $n > 0$ , then

$$\text{wei}(A) = c(R) \times \sum_{i=1}^n c(R_{0i}) \times \text{wei}(A_i).$$

# Interaction: choice between different explanations (cont.)

## Definition (Strength relation)

$A_1$  be an hypothetical argument and  $A_2, A_3$  two built arguments.

- 1  $A_2$  is stronger than  $A_1$  (denoted  $A_2 \succ^A A_1$ );
- 2 If ( $\text{top}(A_2) \sim \text{top}(A_3)$ ) and ( $\text{hypsize}(A_2) \leq \text{hypsize}(A_3)$ ), then  $A_2 \succ^A A_3$ ;
- 3 Else if ( $\text{wei}(A_2) \geq \text{wei}(A_3)$ ), then  $A_2 \succ^A A_3$ ;

# Arguments

Some of the arguments supporting the transport accessibility:

- $B_7^1 = \langle g_7, (D(\text{pisa}), \text{Sea}(\text{pisa})), (D(\text{pisa})) \rangle;$
- $B_7^2 = \langle g_7, (D(\text{pisa}), \text{Road}(\text{pisa})), (D(\text{pisa})) \rangle;$
- $A_7^1 = \langle g_7, (D(\text{london}), \text{Sea}(\text{london})), (D(\text{london}), \text{Sea}(\text{london})) \rangle;$
- $A_7^2 = \langle g_7, (D(\text{london}), \text{Road}(\text{london})), (D(\text{london}), \text{Road}(\text{london})) \rangle.$

Since

- $\text{wei}(B_7^1) = 42/100$ ,  $\text{wei}(B_7^2) = 32/100$ ,  $\text{wei}(A_7^1) = 60/100$ ,  
and  $\text{wei}(A_7^2) = 40/100$ ,
- $\text{hypsize}(B_7^1) = \text{hypsize}(B_7^2) = 1$  and  $\text{hypsize}(A_7^1) =$   
 $\text{hypsize}(A_7^2) = 2$ .

$B_7^1/B_7^2$  defeat  $A_7^1/A_7^2$  and  $B_7^1$  (resp.  $A_7^1$ ) is stronger than  $B_7^2$  (resp.  $A_7^2$ )

$\Rightarrow$  Pisa must be selected as the best alternative to achieve  $g_7$  and the best explanation is based upon the availability of sea transports.

# Semantics

The admissible arguments are:

- $A_0^1 = \langle g_0, (g_1, g_2), (D(\text{london}), \text{Sea}(\text{london})) \rangle;$
- $B_2^1 = \langle g_2, (g_6, g_7), (D(\text{pisa})) \rangle.$

## Definition (Full admissibility)

- $A$  is fully acceptable with respect to  $S$  in  $\mathcal{T}$  (denoted  $A \in \underline{\mathcal{S}}_{\mathcal{A}}^S(\mathcal{T})$ ) iff  $A$  is acceptable with respect to  $S$  in  $\mathcal{T}$  and all its subarguments  $A'$  are acceptable with respect to the set of arguments and subarguments of  $S$  in  $\mathcal{T}_{\text{conc}}(A')$ ;
- $S$  is fully admissible in  $\mathcal{T}$  iff  $S$  is conflict-free and  $\forall A \in S, A \in \underline{\mathcal{S}}_{\mathcal{A}}^S(\mathcal{T})$ ;

The fully admissible arguments are:

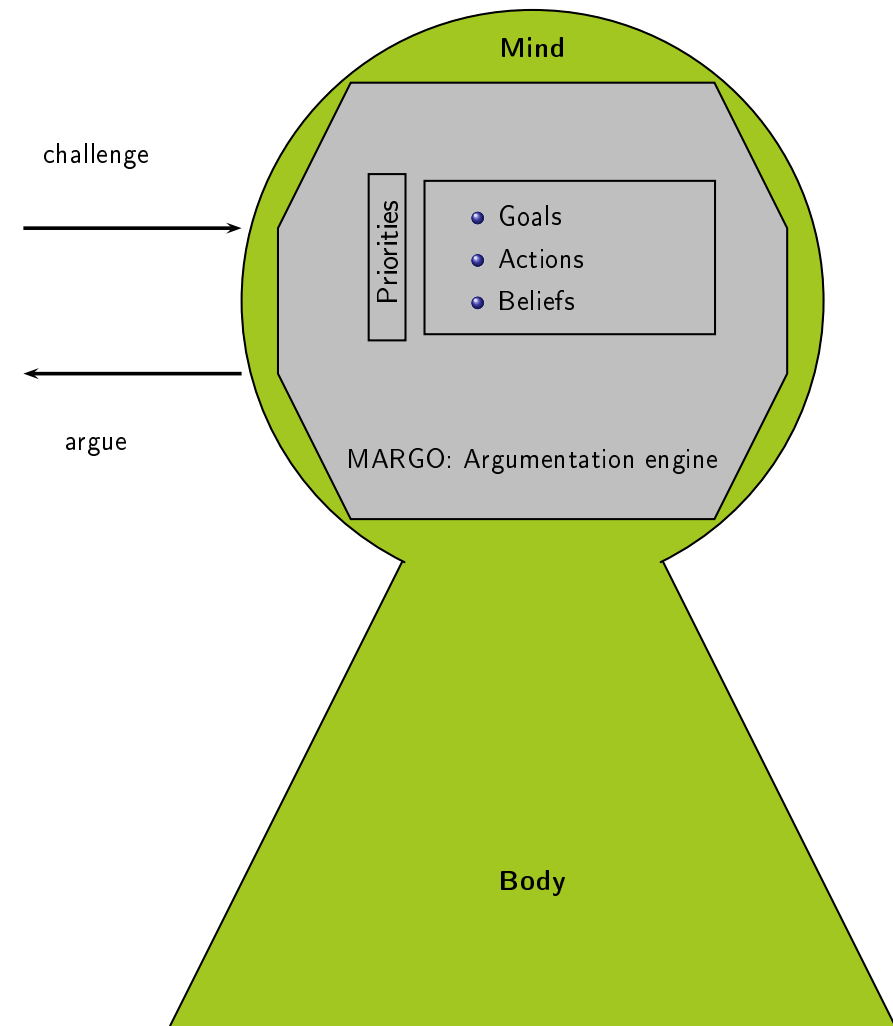
- $A_0^2 = \langle g_0, (g_1), (D(\text{london}), \text{Sea}(\text{london})) \rangle;$
- $B_2^1 = \langle g_2, (g_6, g_7), (D(\text{pisa})) \rangle.$

# Outline

- 1 ARGUGRID
- 2 Argumentation
- 3 Assumption-based argumentation framework
- 4 Argumentation-based decision making
- 5 Quantitative argumentation-based decision making
- 6 Conclusions & Future works**
- 7 Questions ?

# Outlook: Agents' mind (WP2)

- Design
  - state-of-mind (knowledge, goals, actions, plans)
  - qualitative/quantitative priorities
  - workflow in state-of-mind
- Implementation
  - MARGO: a Prolog prototype
- Application
  - procurement/migration/EO scenarios



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[Artificial Intelligence](#), 170(2):114–159, 2006.



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## Brief overview

- Written in Prolog
- Available in GPL at <http://margo.sourceforge.net>
- Built upon CaSAPI (Credulous and Sceptical Argumentation Prolog Implementation) written by Dorian Gaertner and Francesca Toni  
<http://www.doc.ic.ac.uk/~dg00/casapi.html>
- The main procedure is `admissibleArgument(+CONC, -PREMISES, -SUPPOSITIONS)` with:
  - the first argument is the goal/belief of the admissible arguments ie the conclusions;
  - the second argument stands for the premises;
  - the third argument stands for the suppositions.

# A good example is better than a long explanation

```
:- compile('../src/margo.pl').
decisionrule(r71a, g7, [d(london), sea(london)]).
decisionrule(r71b, g7, [d(pisa), sea(pisa)]).
epistemicrule(f11,road(london), []).
epistemicrule(f12,road(pisa), []).
epistemicpriority(f12,f11).
supposition(a11,road(london)).
supposition(a12,road(pisa)).
supposition(a21,sea(london)).
supposition(a22,sea(pisa)).
decisions([d(london), d(pisa)]).
```

admissibleArgument(g7,PREMISES,SUPPOSITION) **returns**

```
PREMISES = [d(london), sea(london)]
SUPPOSITIONS = [d(london), sea(london)] ;
PREMISES = [d(pisa), sea(pisa)]
SUPPOSITIONS = [d(pisa), sea(pisa)] ;
```

# (1) MARGO in the shell: translation in CaSAPI

```

%%%Define CaSAPI rules with priorities/rules
myRule(FACT, [not(del(NAME))]) :- supposition(NAME, FACT).
myRule(HEAD, [not(del(NAME)) | BODY]) :- decisionrule(NAME, HEAD, BODY).
myRule(HEAD, [not(del(NAME)) | BODY]) :- goalrule(NAME, HEAD, BODY).
myRule(HEAD, [not(del(NAME)) | BODY]) :- epistemicrule(NAME, HEAD, BODY).
myRule(del(R1), [not(del(R2))]) :- epistemicpriority(R2, R1).
myRule(del(R1), [not(del(R2))]) :- decisionpriority(R2, R1).

%%%Define set of assumptions with decision/epistemic rules
myAss(Ass) :- findall(D, isDecision(D), DS),
decisionrules(DR), append(DS, DR, SUBA),
epistemicrules(ER), append(ER, SUBA, A),
incompatibilities(I), append(I, A, Ass).

%%%Define CaSAPI's contrary with decisions/incompatibilities
contrary(d(X), d(Y)) :- decisions(D), member(d(X), D), member(d(Y), D), \+ X=Y.
contrary(not(del(X)), del(X)) :- !.
contrary(del(X), not(del(X))).
contrary(X, Y) :- incompatibility(X, Y).
contrary(X, Y) :- incompatibility(Y, X).
contrary(X, Y) :- asincompatibility(Y, X).

```

## (2) MARGO in the shell: CaSAPI meta-interpreter

**Data:** A problem description, a conclusion

**Result:** SENTENCES of an admissible argument

```
myAss(ASSUMPTIONS) ; // set the assumptions
```

```
run(ab,s,a,[CONC],ASSUMPTIONS,SENTENCES) ; // run CaSAPI
```

```
if no argument is found then
```

```
  while strongestrules() do
```

```
    nextstrongerule(TOPRULE) ; // find one of the
```

```
    strongest rule
```

```
    usefulSuppositions(BODY,USL) ; // find minimal non-empty
```

```
    useful hypotheses
```

```
    append(USL,ASSUMPTIONS,NEWASSUMPTIONS);
```

```
    run(ab,s,a,[CONC],NEWASSUMPTIONS,SENTENCES) ;
```

```
    // run CaSAPI with these new assumptions
```

```
  end
```

```
end
```

# Relax of user's needs in CaSAPI

```

%goal rules
myRule(g1,[g4, g5, not(del(r145))]).
myRule(g1,[g4, not(del(r14))]).
myRule(g1,[g5, not(del(r15))]).
%decision rules
myRule(g4,[d(london), not(del(r41))]).
myRule(g4,[d(pisa), not(del(r42))]).
myRule(g5,[d(london), not(del(r51))]).
myRule(g5,[d(pisa), not(del(r52))]).
% decision priorities
myRule(del(r42),[not(del(r41))]).
myRule(del(r51),[not(del(r52))]).

contrary(d(london),d(pisa)).
contrary(d(pisa),d(london)).
contrary(not(del(X)),del(X)) :- !.
contrary(del(X),not(del(X))).

```

```

run(ab,s,a,[g1],[d(pisa), d(london),
not(del(r145)),
not(del(r51)), not(del(r52)),
not(del(r41)), not(del(r42))],X).
says No.

```

```

run(ab,s,a,[g1],[d(pisa), d(london),
not(del(r14)),
not(del(r51)), not(del(r52)),
not(del(r41)), not(del(r42))],X).
says
X = [not(del(r14)), d(london),
not(del(r41))]

```

```

run(ab,s,a,[g1],[d(pisa), d(london),
not(del(r15)),
not(del(r51)), not(del(r52)),
not(del(r41)), not(del(r42))],X).
says
X = [not(del(r15)), d(pisa),
not(del(r52))] ;

```

# Natural relax of user's needs in MARGO

```

%goal rules
goalrule(r145, g1, [g4, g5]).
goalrule(r14, g1, [g4]).
goalrule(r15, g1, [g5]).
%decision rules
decisionrule(r41, g4, [d(london)]).
decisionrule(r42, g4, [d(pisa)]).
decisionrule(r51, g5, [d(london)]).
decisionrule(r52, g5, [d(pisa)]).

%goal priority
goalpriority([[r145],[r14],[r15]]).

%decisio priority
decisionpriority(r41,r42).
decisionpriority(r52,r51).

decisions([d(london), d(pisa)]).

Then argument(g1,PREMISES,SUPPOSTIONS).
PREMISES = [g4]
SUPPOSTIONS = [d(pisa)].

```

# Hypotheses over knowledge in CaSAPI

```

myRule(g7, [d(london), sea(london),
            not(del(r71a))]).
myRule(g7, [d(pisa), sea(pisa),
            not(del(r71b))]).

myRule(sea(pisa), [not(del(supp1))]).
myRule(sea(pisa), [not(del(supp2))]).

contrary(d(london), d(pisa)).
contrary(d(pisa), d(london)).
contrary(not(del(X)), del(X)) :- !.
contrary(del(X), not(del(X))).

```

```

run(ab,s,a,[g7],[d(pisa), d(london),
             not(del(r71a)), not(del(r71b))],X).
says No

```

```

run(ab,s,a,[g7],[d(pisa), d(london),
             not(del(r71a)), not(del(r71b)),
             not(del(supp1)), not(del(supp2))],X).
says
X = [d(pisa), not(del(r71b)),
     not(del(supp1))] ;
X = [d(pisa), not(del(r71b)),
     not(del(supp2))] ;

```

# Natural hypotheses over knowledge in MARGO

```
decisionrule(r71a, g7,
             [d(london), sea(london)]).
```

```
decisionrule(r71b, g7,
             [d(pisa), sea(pisa)]).
```

```
supposition(a11, road(london)).
```

```
supposition(a12, road(pisa)).
```

```
supposition(a21, sea(london)).
```

```
supposition(a22, sea(pisa)).
```

```
decisions([d(london), d(pisa)]).
```

```
argument(g7, PREMISES, SUPPOSITIONS) says
```

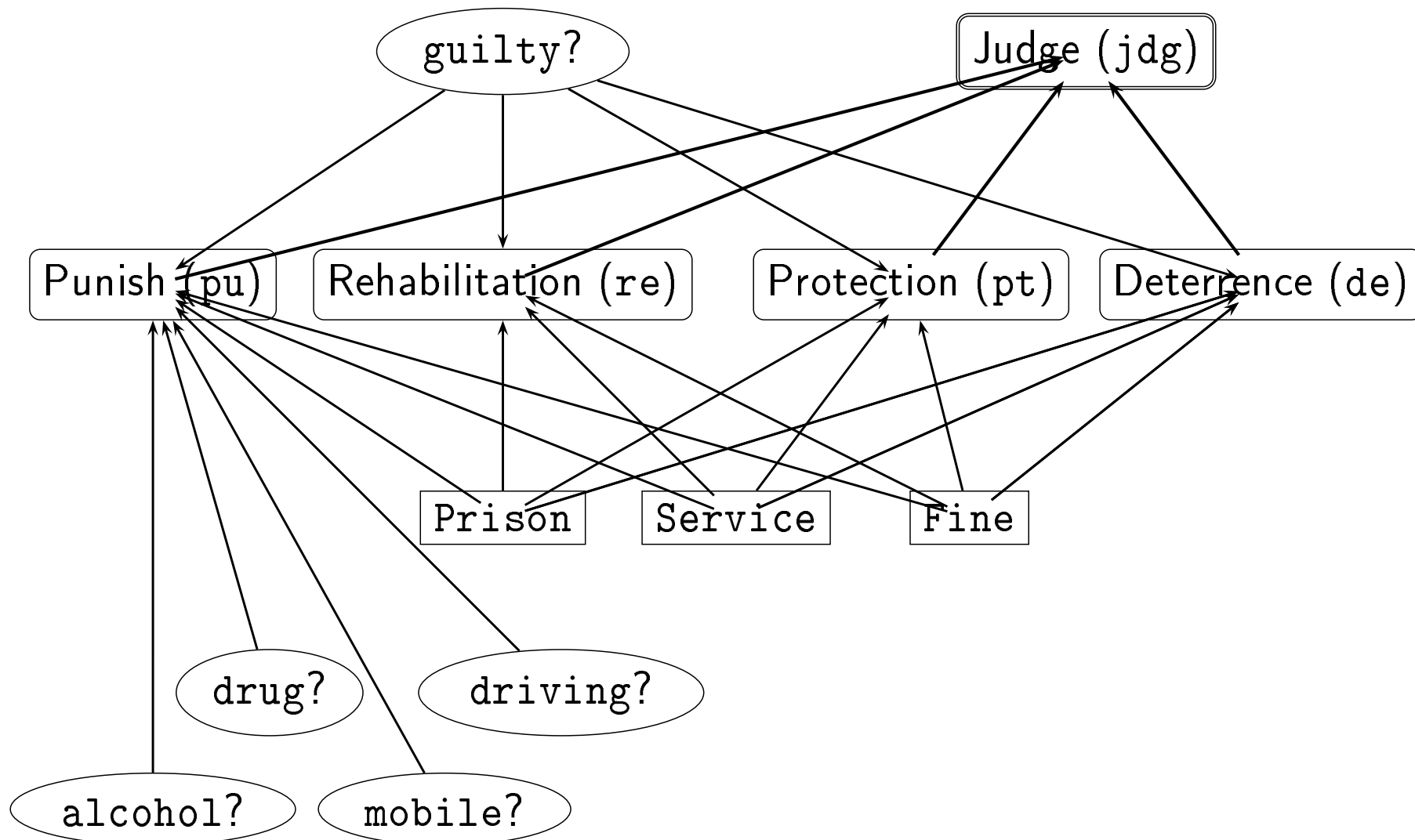
```
PREMISES = [d(london), sea(london)]
```

```
SUPPOSITIONS = [d(london), sea(london)]
```

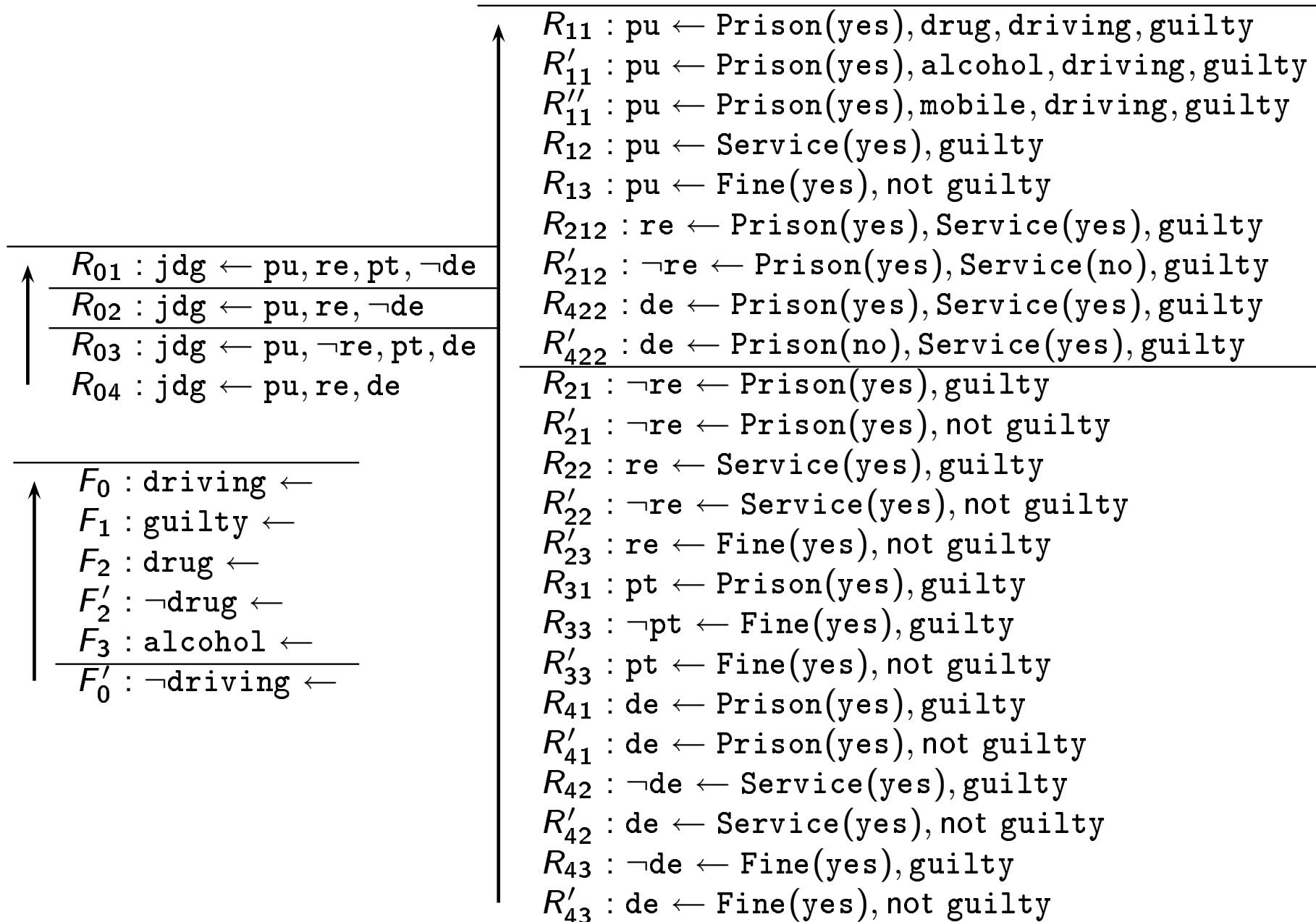
```
PREMISES = [d(pisa), sea(pisa)]
```

```
SUPPOSITIONS = [d(pisa), sea(pisa)]
```

# Influence diagram



# Epistemic/Goal/Decision theory



# Arguments

Some of the arguments concluding  $pu$  are the following:

- $A = \langle re, (Prison(yes), Service(yes), guilty), (Prison(yes), Service(yes)) \rangle;$
- $B = \langle \neg re, (Prison(yes), guilty), (Prison(yes)) \rangle;$
- $C = \langle re, (Service(yes), guilty), (Service(yes)) \rangle;$

Since

- $(top(B) \sim top(C)) \prec top(A),$
- $hypsize(A) = 2$  and  $hypsize(B) = hypsize(C) = 1,$

$A \succ^A B/C.$

$\Rightarrow$  Prison and community service must be selected to promote rehabilitation.